Unit 4 Test Review Honors ICM



Name:

Period:

Find the derivative of the function using the limit definition of derivative. Show all work!

1.
$$f(x) = 2x + 4$$

2. $f(x) = \frac{2}{x+3}$

3.
$$f(x) = \sqrt{x+6}$$
 4. $f(x) = 3x^2 - x + 2$

Find the equation for the tangent line at the given point.

5.
$$f(x) = x^2 + 3x - 1;$$
 (1,3)
6. $f(x) = \frac{1 + x^2}{x + 5};$ (0, $\frac{1}{5}$)

7.
$$f(x) = -4x + 3$$
; $x = -1$
8. $f(x) = -5x^2 + 8x + 2$; $x = 3$

9.
$$f(x) = (x^3 + 2)(2x^2 - 4);$$
 (1,2)
10. $f(x) = \frac{1}{x^2};$ (-1,1)

Find the slope of the tangent line to the graph of *f* at a given point.

11.
$$f(x) = (4x^3 - 5x^2)(1 + 2x);$$
 (-1,7)
12. $f(x) = \frac{2x - 3x^2}{5x + 1};$ $x = 2$

13.
$$f(x) = \frac{6}{x+1}$$
; $x = 2$
14. $f(x) = 3x^4 - 6x^2 + 5x - 4$; (-2,8)

15. The displacement *s* (in meters) of a particle moving in a straight line is given by the equation of motion $s = 4t^3 + 6t + 2$, where *t* is measure in seconds. Find the instantaneous velocity of the particle *s* at times t = a, t = 1, and t = 3.

- 16. If an arrow is shot upward on the moon with a velocity of 58 miles/s, its height (in meters) after t seconds is given by $H = 58t .83t^2$. The moon is at the maximum.
 - a) Find the instantaneous velocity of the arrow after 1 second.
 - b) At what time t will the arrow hit the moon?
 - c) With what velocity will the arrow hit the moon?

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17. The position of a particle at time t sec is $s = t^3 - 6t^2 + 9t$ meters.

- (a) Find the instantaneous velocity t = 4 seconds.
- (b) Find the acceleration for each time the particle's velocity is zero.

18. A projectile is shot upward from the surface of earth with an initial velocity of 120 meters per second. The position

equation is $s(t) = -4.9t^2 + 120t$

- a. What is the projectile's velocity after 5 seconds?
- b. What is the projectile's acceleration after 5 seconds?

Find the derivative.

19.
$$f(x) = 9x^{-2} + \sqrt{2x^5 - x^3}$$

20. $f(x) = \frac{2}{5x^2}$
21. $g(x) = 3x^2 - \sqrt[4]{x^3}$

22.
$$h(x) = (x^3 - 7)(2x^3 + 3)$$
 23. $f(x) = (2x^2 - 4x + 1)(6x - 5)$

24.
$$f(x) = x^{\frac{3}{2}}(3x^2 - 2x + 6)$$
 25. $g(x) = 12x^{\frac{3}{5}} + \sqrt[3]{2x^4 - 4x}$

26.
$$f(x) = (x^5 - 2x^3)(7x^2 + x - 8)$$
 27. $h(x) = \frac{5x - 6}{3x + 7}$

28.
$$f(x) = \frac{6 - x + 3x^2}{4 - 9x}$$
 29. $f(x) = \frac{x^3 + 1}{x^3 - 1}$

30.
$$h(x) = \left(\frac{3x+4}{6x-1}\right)^3$$
 31. $g(x) = \frac{\sqrt[3]{x^2}}{3x-5}$