

# Unit 4 Review Day

# Warm Up:

$$f(x) = \frac{x^2 - 4}{2x^2 + 11x + 14}$$

Domain:	Range:	Vertical Asymptote:	Horizontal Asymptote:	Removable POINT:
X-intercept:	Y-intercept:	Increasing:	Decreasing:	Hole:
Infinite discont.:	$\lim_{x \rightarrow \infty} f(x)$	$\lim_{x \rightarrow -\infty} f(x)$	$\lim_{x \rightarrow -2} f(x)$	$\lim_{x \rightarrow -\frac{7}{2}} f(x)$
Absolute Min:	Absolute Max:	Relative Min:	Relative Max:	Continuous?

# Warm Up:

$$f(x) = \frac{x^2 - 4}{2x^2 + 11x + 14}$$

<b>Domain:</b> $(-\infty, -\frac{7}{2}) \cup (-\frac{7}{2}, -2)$ $\cup (-2, \infty)$	<b>Range:</b> $(-\infty, -\frac{4}{3}) \cup (-\frac{4}{3}, \frac{1}{2})$ $\cup (\frac{1}{2}, \infty)$	<b>Vertical Asymptote: x</b> <b>= -7/2</b>	<b>Horizontal Asymptote:</b> <b>y=1/2</b>	<b>Removable POINT:</b> <b>(-2, -4/3)</b>
<b>X-intercept:</b> <b>(2, 0)</b>	<b>Y-intercept:</b> <b>(0, -2/7)</b>	<b>Increasing:</b> $(-\infty, -\frac{7}{2}) \cup (-\frac{7}{2}, -2)$ $\cup (-2, \infty)$	<b>Decreasing:</b> <b>NONE</b>	<b>Hole:</b> <b>(-2, -4/3)</b>
<b>Infinite discontin.:</b> <b>X=-7/2</b>	$\lim_{x \rightarrow \infty} f(x)$ <b>1/2</b>	$\lim_{x \rightarrow -\infty} f(x)$ <b>1/2</b>	$\lim_{x \rightarrow -2} f(x)$ <b>-4/3</b>	$\lim_{x \rightarrow -\frac{7}{2}} f(x)$ <b>DNE</b>
<b>Absolute Min:</b> <b>NONE</b>	<b>Absolute Max:</b> <b>NONE</b>	<b>Relative Min:</b> <b>NONE</b>	<b>Relative Max:</b> <b>NONE</b>	<b>Continuous?</b> <b>NO!</b>

# Questions on last night's HW?

- ▶ Packet p. 10-12

## Tonight's HW

- ▶ Test Review sheet (Potatoes one)

# Unit 4 Summary

Domain: Consider the **vertical asymptotes** and the **x-value** of the **hole (if they exist)** and **x-intercept** (esp. for sq. roots)

Range: Consider the **horizontal asymptotes** and the **y-value** of the **hole (if they exist)** and **x-intercept** (esp. if HA:  $y = 0$ )

Limits: Consider holes, horizontal asymptotes, end behavior

x-intercept: Set  $y = 0$  and solve for  $x$ .

y-intercept: Set  $x = 0$  and solve for  $y$ .

Min/Max:

Y-value occurs at x-value

Inc/Dec:

Write in terms of x-values!

Use brackets for max/min

# Unit 4 Summary (continued)

A function is **EVEN** if  $f(-x) = f(x)$  -> Symm. over y-axis

A function is **ODD** if  $f(-x) = -f(x)$  -> Symm. about origin

## Combinations and Compositions

▶ Add:  $(f + g)(x) = f(x) + g(x)$

▶ Subtract:  $(f - g)(x) = f(x) - g(x)$

▶ Multiply:  $(f \cdot g)(x) = f(x) \cdot g(x)$

▶ Divide:  $(f/g)(x) = f(x)/g(x)$

$(f \circ g)(x) = f(g(x))$  \*consider domain of  $g(x)$  and  $f(g(x))$

$(g \circ f)(x) = g(f(x))$  \*consider domain of  $f(x)$  and  $g(f(x))$

# More Limits Practice Sheet

# Test Review Scavenger Hunt Game





# Quiz Corrections

- ▶ On a NEW sheet of notebook paper
- ▶ Required if below 80% on Quiz
- ▶ Use table format (see side board)
  
- ▶ Show your work for completing them (graph, diagram, etc), NOT just answers!
- ▶ Ask questions
  
- ▶ When done, work on Test Review HW! 😊

- ▶ Phones stay in the **red pockets** until you are completely finished with the Review HW and Quiz Corrections!

Next slides used earlier for Fall '18

# Limits Algebraically Practice Sheet

Practice Continues ->

# Warm-Up Review Day!

1. Write an equation of a rational function with Removable Discontinuity at 7, Non-Removable Discontinuity at -2, and Horizontal Asymptote of  $y = 3/4$

2. State the following and graph

▶ Domain:

▶ Range:

▶ x & y intercepts:

▶ Removable Discontinuity:

▶ Non-Removable Discontinuity:

▶ Horizontal Asymptote:

▶ Limits at discontinuities:

▶ End Behavior using limits:

$$g(x) = \frac{2x^2 - 10x + 8}{4x^2 - 4x}$$

# Warm-Up      Answers

1. Write an equation of a rational function with Removable Discontinuity at 7, Non-Removable Discontinuity at -2, and Horizontal Asymptote of  $y = 3/4$

*Example :*

$$f(x) = \frac{3x(x-7)}{4(x-7)(x+2)}$$

# Warm-Up ANSWERS ~

$$g(x) = \frac{2x^2 - 10x + 8}{4x^2 - 4x}$$

$$= \frac{2(x^2 - 5x + 4)}{4x(x-1)}$$

$$= \frac{2(x-4)(x-1)}{4x(x-1)}$$

State the following and graph

- ▶ Domain:  $(-\infty, 0) \cup (0, 1) \cup (1, \infty)$
- ▶ Range:  $(-\infty, -3/2) \cup (-3/2, 1/2) \cup (1/2, \infty)$
- ▶ x & y intercepts: **x-int: (4, 0)**      **y-int: NONE**
- ▶ Removable Discontinuity: **Hole: (1, -3/2)**
- ▶ Non-Removable Discontinuity: **VA: x = 0**
- ▶ Horizontal Asymptote: **HA: y = 1/2**
- ▶ Limits at discontinuities:  $\lim_{x \rightarrow 1} f(x) = -3/2$        $\lim_{x \rightarrow 0} f(x) = DNE$
- ▶ End Behavior using limits:  $\lim_{x \rightarrow \infty} f(x) = 1/2$        $\lim_{x \rightarrow -\infty} f(x) = 1/2$

# Practice Review Day

Using the graph of  $f(x)$  below, find the following limits.

1.  $\lim_{x \rightarrow -5} f(x)$

2.  $\lim_{x \rightarrow -3} f(x)$

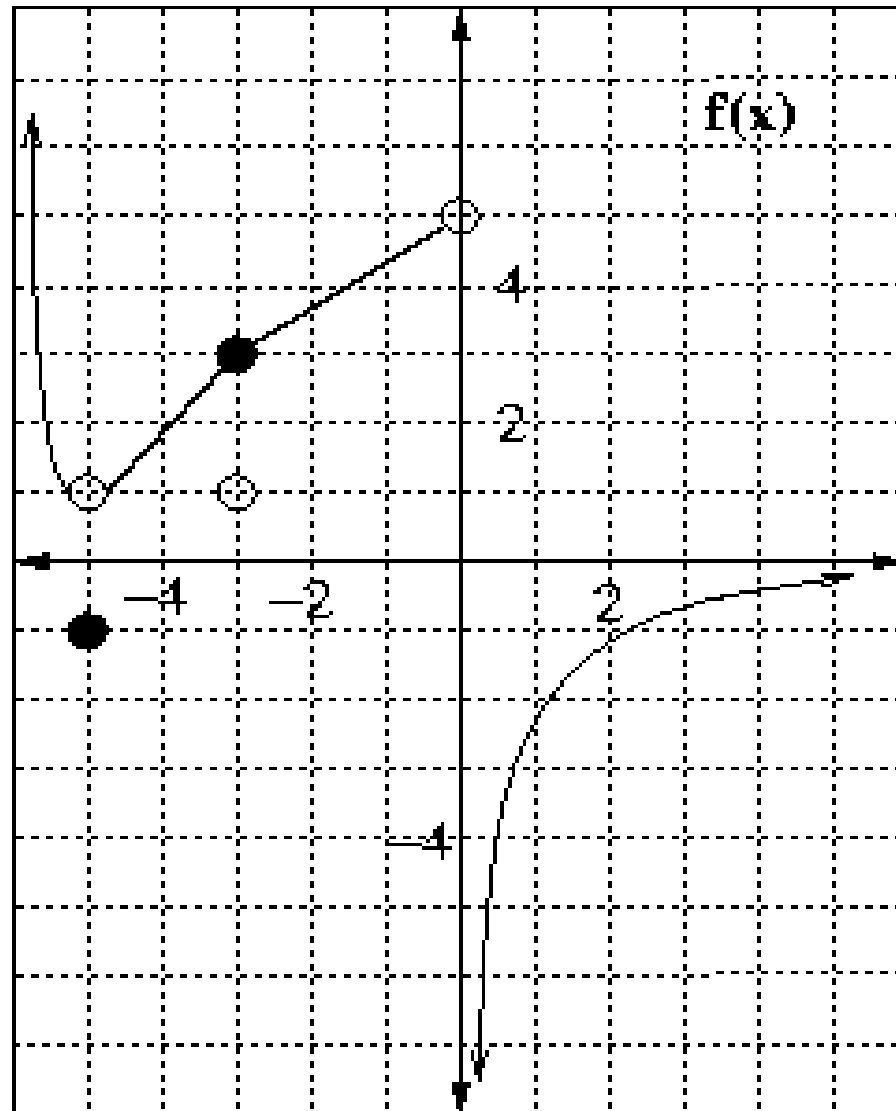
3.  $\lim_{x \rightarrow -\infty} f(x)$

4.  $\lim_{x \rightarrow 0^-} f(x)$

5.  $\lim_{x \rightarrow \infty} f(x)$

6.  $\lim_{x \rightarrow 0} f(x)$

7.  $f(-5)$



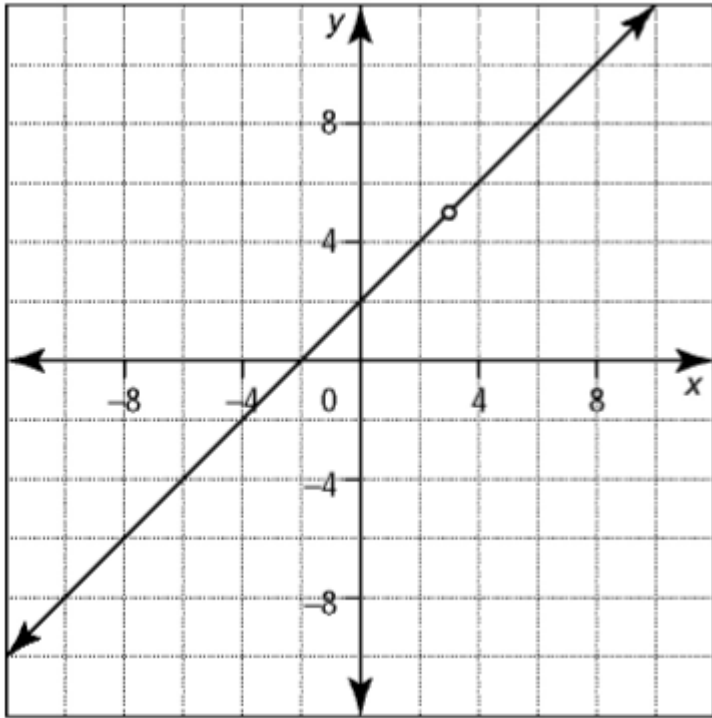
Practice Continues ->



# Practice Review Day (continued)

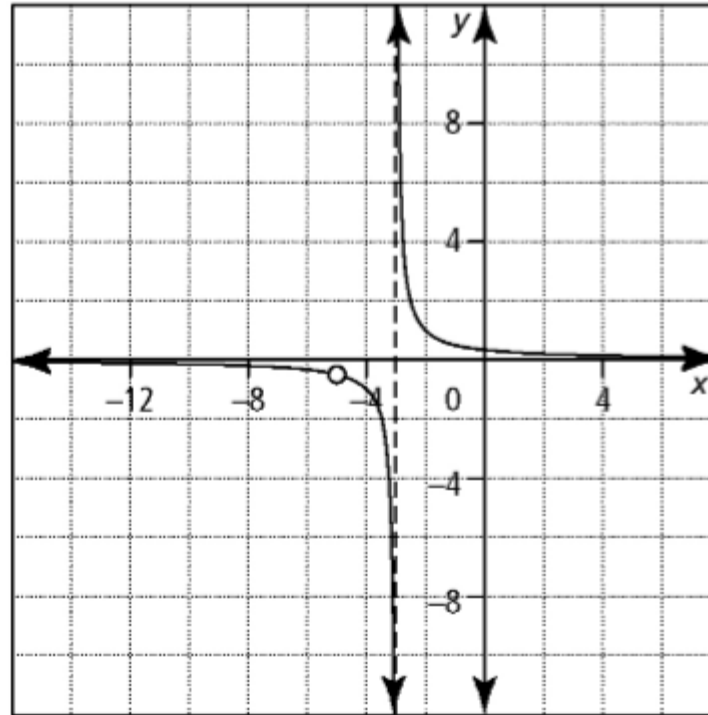
Write an equation for the graphed rational function.

8.



Hole (3, 5)

9.

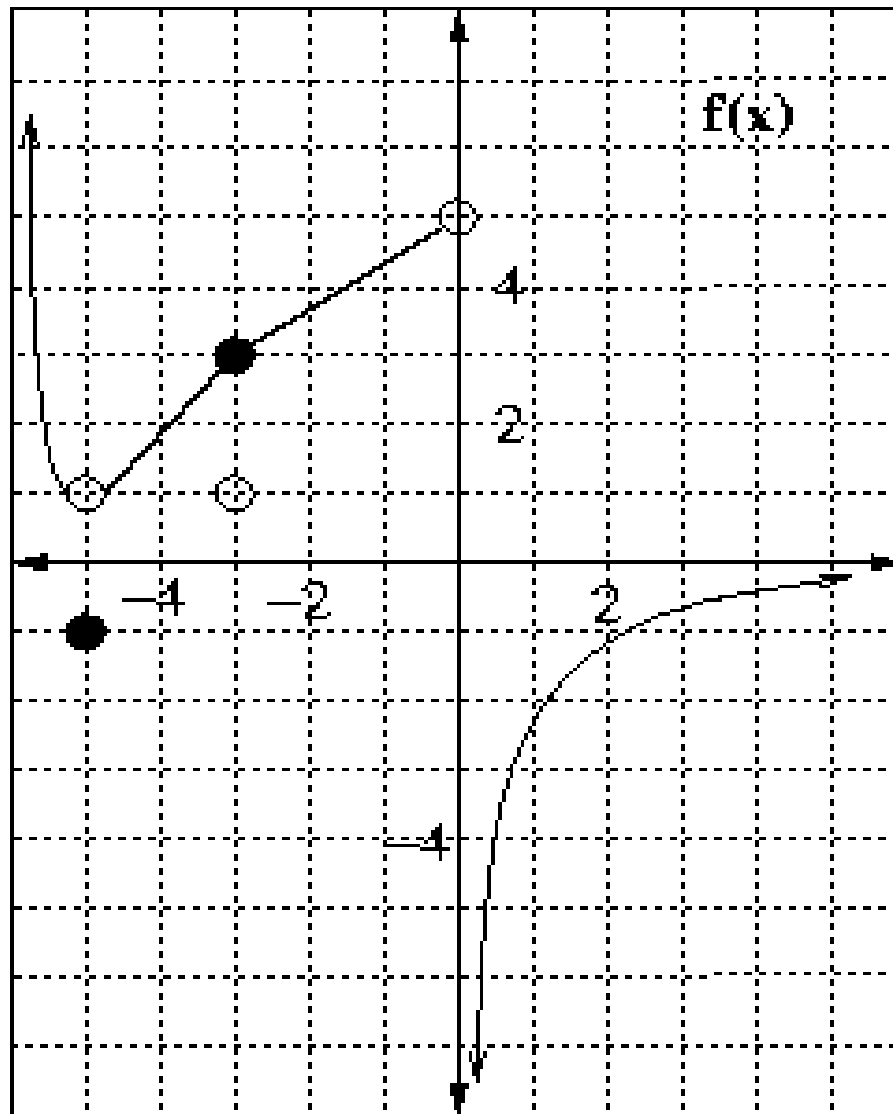


Hole (-5, -1/2)

# Practice Review Day: ANSWERS

Using the graph of  $f(x)$  below, find the following limits.

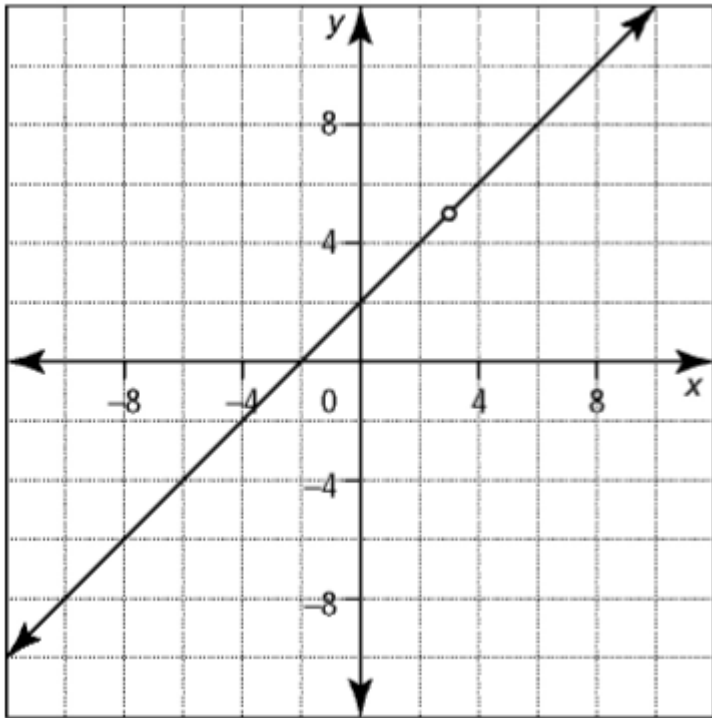
1.  $\lim_{x \rightarrow -5} f(x) = 1$
2.  $\lim_{x \rightarrow -3} f(x) = 3$
3.  $\lim_{x \rightarrow -\infty} f(x) = \infty$
4.  $\lim_{x \rightarrow 0^-} f(x) = 5$
5.  $\lim_{x \rightarrow \infty} f(x) = 0$
6.  $\lim_{x \rightarrow 0} f(x) = DNE$
7.  $f(-5) = -1$



# Practice Review Day: ANSWERS

Write an equation for the graphed rational function.

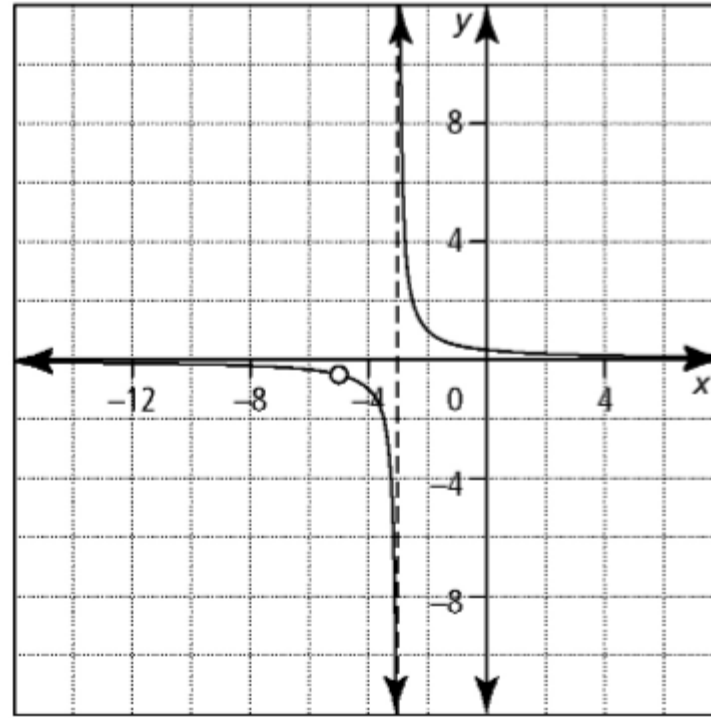
8.



Hole (3, 5)

$$y = \frac{(x - 3)(x + 2)}{(x - 3)}$$

9.



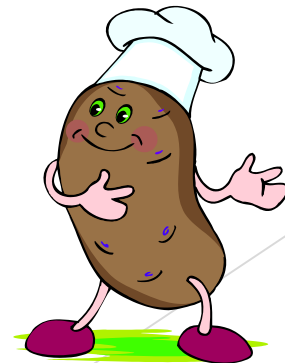
Hole (-5, -1/2)

$$y = \frac{(x + 5)}{(x + 5)(x + 3)}$$

# Mr. Potato Head Review

With your assigned group of 3 or 4

- ▶ 1 person can pick up a set of questions and a Mr. Potato Head
- ▶ After you complete each set, you may check your answers with me. If all are correct, you will choose 1 piece to add to Mr. Potato Head
- ▶ We will judge the best Mr. Potato Head at the end of class!



# Midterm Review Packet

Using the graph of  $f(x)$  below, find the following limits.

1.  $\lim_{x \rightarrow 1} f(x)$

2.  $\lim_{x \rightarrow 1^-} f(x)$

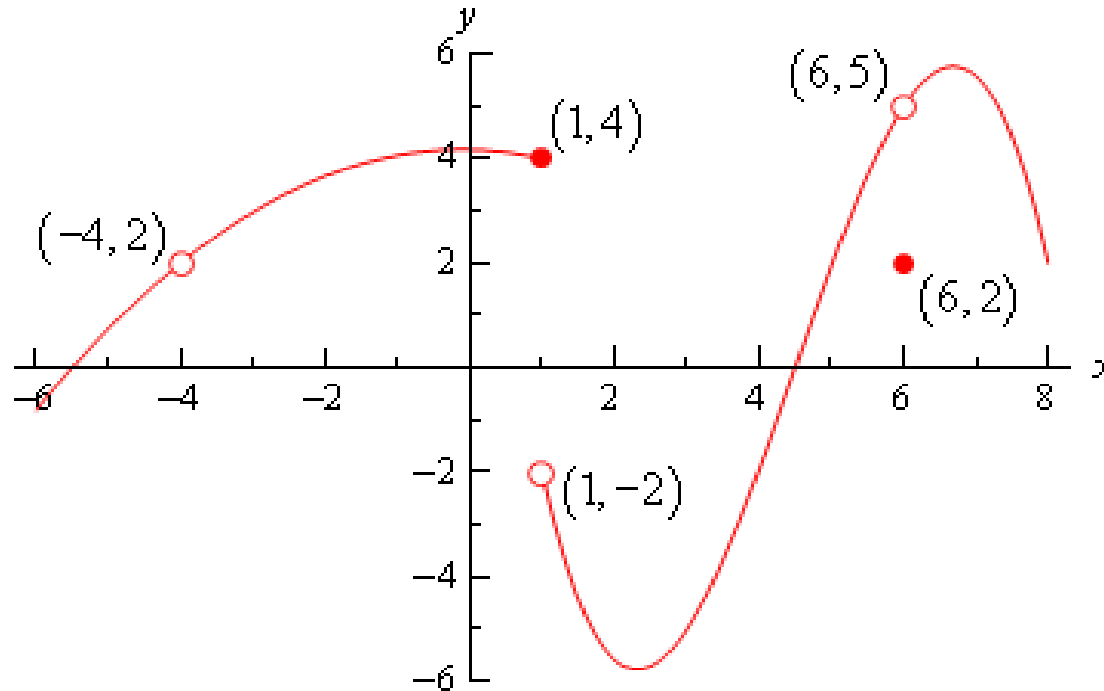
3.  $\lim_{x \rightarrow -4} f(x)$

4.  $\lim_{x \rightarrow -\infty} f(x)$

5.  $\lim_{x \rightarrow \infty} f(x)$

6.  $\lim_{x \rightarrow 6} f(x)$

7.  $f(6)$



Practice Continues ->

## Practice ~

$$g(x) = \frac{\sqrt[3]{x}}{x^2 - x}$$

State the following and make a graph

- ▶ Domain:
- ▶ Range:
- ▶ x & y intercepts:
- ▶ Max and Min:
- ▶ Increasing:
- ▶ Decreasing:
- ▶ Limits at discontinuities:
- ▶ End Behavior using limits:

# Practice ANSWERS ~

$$g(x) = \frac{\sqrt[3]{x}}{x^2 - x}$$

State the following and sketch a graph

► Domain:  $(-\infty, 0) \cup (0, 1) \cup (1, \infty)$     **VA:  $x = 0$  &  $x = 1$**

► Range:  $(-\infty, 0) \cup (0, \infty)$

► x & y intercepts: NONE

► Max and Min: *max of  $-3.07$  at  $x = 0.4$ ; min.: none*

► Increasing:  $(0, 0.4]$

► Decreasing:  $(-\infty, 0) \cup [0.4, 1) \cup (1, \infty)$

► Limits at discontinuities:  $\lim_{x \rightarrow 0} f(x) = -\infty$

$\lim_{x \rightarrow 1} f(x) = DNE$

► End Behavior using limits:

$$\lim_{x \rightarrow \infty} f(x) = 0$$

$$\lim_{x \rightarrow -\infty} f(x) = 0$$

To see the Max and the two VAs, adjust window:

X-min: -5    X-max: 5

Y-min: -5    Y-max: 5