



UNIT 1 DAY 9

PROBABILITY LAB

LET'S PLAY WITH DICE AND CARDS



WARM UP DAY 9

1. LET A AND B BE EVENTS SUCH THAT
 $P(A \cap B) = 0.25$ $P(A^c) = 0.4$ $P(B) = 0.5$

A) WHAT IS $P(A \cup B)$?

B) WHAT IS $P(A^c \cap B^c)$?

2. LIST THE EVENTS, E, OF GETTING TAILS FIRST OR LAST OR BOTH, IN 3 TOSSES OF A FAIR COIN? WHAT IS THE PROBABILITY OF E?

3. A MONTH IS CHOSEN FROM A YEAR. WHAT IS THE PROBABILITY OF CHOOSING A MONTH THAT STARTS WITH A J OR HAS EXACTLY 30 DAYS?

Grab a Little Whiteboard
for later! 😊

**RIDDLE: I TRAVEL ALL OVER THE WORLD, BUT
ALWAYS STAY IN MY CORNER. WHAT AM I?**

Remember to Pick
up the Quiz #2
Review Handout
from the crate if
you missed it
yesterday! 😊

WARM UP ANSWERS

1. LET A AND B BE EVENTS SUCH THAT:

$$P(A \cap B) = 0.25 \quad P(A^c) = 0.4 \quad P(B) = 0.5$$

WHAT IS $P(A \cup B)$? **0.85**

WHAT IS $P(A^c \cap B^c)$? **0.15**

2. LIST THE EVENTS, E, OF GETTING TAILS FIRST OR LAST OR BOTH, IN 3 TOSSES OF A FAIR COIN? WHAT IS THE PROBABILITY OF E?

$$E = \{HHT\}, \{HTT\}, \{THH\}, \{THT\}, \{TTH\}, \{TTT\}$$

$$P(E) = 6/8 = \mathbf{3/4 = 0.75}$$

3. A MONTH IS CHOSEN FROM A YEAR. WHAT IS THE PROBABILITY OF CHOOSING A MONTH THAT STARTS WITH A J OR HAS EXACTLY 30 DAYS?

$$\mathbf{3/12 + 4/12 - 1/12 = 1/2 \text{ or } 0.50}$$

RIDDLE OF THE DAY!

- **I TRAVEL ALL OVER THE WORLD, BUT ALWAYS STAY IN MY CORNER. WHAT AM I?**
- **A STAMP!**

HW QUESTIONS????

HW: FINISH

- QUIZ #2 REVIEW SHEET
- REVIEW QUIZ #1 AND PRE-ASSESSMENT
→ SOME QUIZ 2 TOPICS BUILD UPON THAT MATERIAL! 😊

WHITEBOARD PRACTICE

PRACTICE

4. IN THE MATH CLUB, 7 OF THE 20 GIRLS ARE SENIORS, AND 4 OF THE 14 BOYS ARE SENIORS. WHAT IS THE PROBABILITY OF RANDOMLY SELECTING A BOY OR A SENIOR TO REPRESENT THE MATH CLUB AT A STATEWIDE MATH CONTEST?

PRACTICE ANSWERS

4. IN THE MATH CLUB, 7 OF THE 20 GIRLS ARE SENIORS, AND 4 OF THE 14 BOYS ARE SENIORS. WHAT IS THE PROBABILITY OF RANDOMLY SELECTING A BOY OR A SENIOR TO REPRESENT THE MATH CLUB AT A STATEWIDE MATH CONTEST?

$$14/34 + 11/34 - 4/34 = 21/34$$

PRACTICE

5. GIVEN $S = \{6, 7, 8, 9, W, X, Y, Z\}$, $A = \{6, 8, X, Z\}$, AND
 $B = \{6, X, Y\}$

A) $A^c \cap B$

B) $A^c \cup B$

PRACTICE ANSWERS

5. GIVEN $S = \{6, 7, 8, 9, W, X, Y, Z\}$, $A = \{6, 8, X, Z\}$, AND $B = \{6, X, Y\}$

A) $A^c \cap B = \{Y\}$

In $\{7, 9, W, Y\}$ AND $\{6, X, Y\}$

B) $A^c \cup B = \{6, 7, 9, W, X, Y\}$

$\{7, 9, W, Y\}$ OR $\{6, X, Y\}$

PRACTICE

6. EVALUATE $F(X - 7) + 5$ GIVEN $F(X) = X^2 + 13$

PRACTICE ANSWERS

6. EVALUATE $F(X - 7) + 5$ GIVEN $F(X) = X^2 + 13$

$$(x - 7)^2 + 13 + 5$$

$$(x - 7)(x - 7) + 18 = x^2 - 14x + 67$$

EXTRA PRACTICE

7. A BAG OF CANDY CONSISTS OF 6 SNICKERS AND 12 TWIX. YOU DRAW 2 PIECES OF CANDY OUT OF THE BAG, ONE AFTER THE OTHER. WHAT IS THE PROBABILITY THAT YOU DRAW AT LEAST 1 TWIX?



EXTRA PRACTICE ANSWER

7. A BAG OF CANDY CONSISTS OF 6 SNICKERS AND 12 TWIX. YOU DRAW 2 PIECES OF CANDY OUT OF THE BAG, ONE AFTER THE OTHER. WHAT IS THE PROBABILITY THAT YOU DRAW AT LEAST 1 TWIX?

$$P(\geq 1 \text{ Twix}) = 1 - P(\text{none})$$

$$1 - \left(\frac{6}{18} \cdot \frac{5}{17}\right)$$

$$1 - \frac{5}{51} = 0.9020$$



$$P(T, T) + P(T, S) + P(S, T)$$

$$\frac{12}{18} \cdot \frac{11}{17} + \frac{12}{18} \cdot \frac{6}{17} + \frac{6}{18} \cdot \frac{12}{17}$$

$$0.431 + 0.235 + 0.235 = 0.9020$$

EXTRA PRACTICE

8. THE PROBABILITY OF A MUDSLIDE IN A PARTICULAR TOWN IN CALIFORNIA IS 12 PERCENT. WHAT IS THE PROBABILITY THEY WILL HAVE AT LEAST ONE MUDSLIDE IN THE NEXT TWENTY YEARS?



EXTRA PRACTICE ANSWERS

8. THE PROBABILITY OF A MUDSLIDE IN A PARTICULAR TOWN IN CALIFORNIA IS 12 PERCENT. WHAT IS THE PROBABILITY THEY WILL HAVE AT LEAST ONE MUDSLIDE IN THE NEXT TWENTY YEARS?

$$\begin{aligned}P(\text{at least 1 mudslide}) &= 1 - P(\text{none}) \\&= 1 - (.88)^{20} \\&= 0.9224\end{aligned}$$



EXTRA PRACTICE

9. FOR A SHIFT AT WORK, IN HOW MANY WAYS CAN YOU CHOOSE A MANAGER AND ASSISTANT MANAGER, 5 CASHIERS AND 3 STOCKERS. THERE ARE 4 MANAGERS, 12 CASHIERS AND 8 STOCKERS ON STAFF.



EXTRA PRACTICE ANSWERS

9. FOR A SHIFT AT WORK, IN HOW MANY WAYS CAN YOU CHOOSE A MANAGER AND ASSISTANT MANAGER, 5 CASHIERS AND 3 STOCKERS. THERE ARE 4 MANAGERS, 12 CASHIERS AND 8 STOCKERS ON STAFF.

$$\begin{aligned} &= {}_4P_2 * {}_{12}C_5 * {}_8C_3 \\ &= 12 * 792 * 56 \\ &= 532,224 \end{aligned}$$



EXTRA PRACTICE

10. In how many ways can you rearrange “classrooms”?



EXTRA PRACTICE ANSWERS

10. In how many ways can you rearrange “classrooms”?

$$= \frac{10!}{(3! 2!)} = 302,400$$



REMINDERS ABOUT PROBABILITY

- PROBABILITY DESCRIBES THE CHANCE THAT AN UNCERTAIN EVENT WILL OCCUR.
- NOTATION: P(E) MEANS PROBABILITY OF EVENT E OCCURRING.

$$\frac{\text{desired \#}}{\text{total \#}}$$

Theoretical Probability =
what **SHOULD** happen,
in theory

$$\frac{\text{\# of ways desired event E occurs}}{\text{total \# in sample space}}$$

Empirical Probability =
what **ACTUALLY**
happened
in an **experiment**

$$\frac{\text{\# of ways desired event E occurs}}{\text{\# of total trials}}$$

PROBABILITY LAB



- **EACH PERSON MUST DO A LAB SHEET, BUT YOU WILL WORK WITH YOUR PARTNER.**
- **1ST, FIND THE THEORETICAL PROBABILITIES FOR THE DICE AND CARDS.**
- **2ND, BRING YOUR THEORETICAL ANSWERS TO ME TO CHECK.**
- **3RD, ONE ROLLS/DRAWS AND THE OTHER PARTNER WRITES. THEN EACH RECORDS THE DATA.**
- **4TH, FIND YOUR EMPIRICAL (EXPERIMENTAL) DATA ANSWERS AND COMPARE THEM TO THE THEORETICAL.**

HW: FINISH

- QUIZ #2 REVIEW SHEET
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CHANGED FORMAT OF LESSON STARTING SPRING 19

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10. IN HOW MANY WAYS CAN YOU REARRANGE "CLASSROOMS"?

